

8.1 Practice Problems Adapted from AP Classroom (non secure).

1. The average value of a function f over the interval $[-1,2]$ is -4 , and the average value of f over the interval $[2,7]$ is 8 . What is the average value of f over the interval $[-1,7]$?

2. The average value of a function f over the interval $[-2,3]$ is -6 , and the average value of f over the interval $[3,5]$ is 20 . What is the average value of f over the interval $[-2,5]$?

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3. Find the average value of f on the interval $-4 \leq x \leq 4$? $f(x) = \sqrt{16 - x^2}$.

4. A store is having an all-day sale. The total number of shoppers who have entered the



store t hours after the store opens is modeled by the function S defined by

$S(t) = 0.5t^4 - 16t^3 + 144t^2$ for $0 \leq t \leq 12$. At time $t = 0$, when the store

opens, there are no shoppers in the store. Find the value of $\frac{1}{3} \int_6^9 S'(t) dt$. Using correct

units, explain the meaning of $\frac{1}{3} \int_6^9 S'(t) dt$ in the context of this problem.

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5. If the average value of a continuous function f on the interval $[-1, 11]$ is 5, what is

$$\int_{-1}^{11} \frac{f(x)}{6} dx ?$$

6. Let f be the function that is defined for all real numbers x and that has the following properties.


(i) $f''(x) = 24x - 18$

(ii) $f'(1) = -6$

(iii) $f(2) = 0$

Find the average value of f on the interval $1 \leq x \leq 3$.

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7. Grass clippings are in a bin where they decompose. For $0 \leq t \leq 10$, the amount of  grass clippings remaining in the bin is modeled by $A(t) = 7(0.9)^t$, where $A(t)$ is measured in pounds and t is measured in days.

Find the time t for which the amount of grass clippings in the bin is equal to the average amount of grass clippings in the bin over the interval $0 \leq t \leq 10$.

8. The average value of $y = \frac{1}{x}$ on the closed interval $[1, 3]$ is ?

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9. What is the average value of $y = x^2\sqrt{x^3 + 1}$ on the interval $[0, 2]$?

10. The average value of $y = \sqrt{x}$ over the interval $0 \leq x \leq 2$ is ?

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11. What is the average (mean) value of $y = 3t^3 - t^2$ over the interval $-1 \leq t \leq 2$?

12. What is the average value of $y = \frac{x}{x^2+2}$ on the interval $0 \leq x \leq \sqrt{6}$.

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13. Let f be the function defined by $f(x) = \begin{cases} \sqrt{x+1} & \text{for } 0 \leq x \leq 3 \\ 5-x & \text{for } 3 < x \leq 5 \end{cases}$.

Find the average value of $f(x)$ on the closed interval $0 \leq x \leq 5$.

14. What is the average value for the portion of the curve $y = 3x - x^2$, which is in Quadrant I of the coordinate plane?

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Answers:

1. $\frac{7}{2}$

2. $\frac{10}{7}$

3. π

4. $\frac{1}{3} \int_6^9 S'(t) dt = 301.5$; $\frac{1}{3} \int_6^9 S'(t) dt$ is the average rate at which the shoppers are entering the store in shoppers/hr between times $t = 6$ and $t = 9$ hours.

5. 10

6. 5

7. The average value, 4.327 pounds, occurs at $t = 4.565$ days.

8. $\frac{\ln 3}{2}$

9. $\frac{26}{9}$

10. $\frac{2}{3}\sqrt{2}$

11. $\frac{11}{4}$

12. $\frac{1}{\sqrt{6}} \ln 2$

13. $\frac{4}{3}$

14. $\frac{3}{2}$