## Contextual Applications of Differentiation UNIT 4 REVIEW

AP Calc April 16, 2020

- 4.1 Interpreting the Meaning of the Derivative in Context
- 4.2 Straight-Line Motion: Connecting Position, Velocity and Acceleration \*\* WATCH AP LIVE #10 "8.2" \*\*
- 4.3 Rates of Change in Applied Contexts Other Than Motion
- 4.4 Introduction to Related Rates / 4.5 Solving Related Rates Problems
- 4.6 Tangent Line Approximations
- 4.7 L'Hospital's Rule (sometimes L'Hôpital's)
- 4.1 The function C(x) gives the cost of digging a hole x feet deep.

C(20) = 140 means that a hole \_\_\_\_\_\_ deep costs \_\_\_\_\_ to dig.

C'(20) = 5 means that when the hole is \_\_\_\_\_\_, the cost of digging is \_\_\_\_\_\_ a rate of .

4.2 A particle moves back and forth on a horizontal track for  $0 \le t < \frac{\pi}{2}$  minutes. The particle's position, in feet, is given by the function  $s(t) = \frac{1}{2} \tan t$ . Find the acceleration of the particle at time  $t = \frac{\pi}{6}$  minutes and indicate units of measure.

If P(t) models the size of a population at time t > 0, which of the following differential equations describes linear growth in the size of the population? Which describes exponential growth?  $\frac{dP}{dt} = 200 \qquad \frac{dP}{dt} = 200t \qquad \frac{dP}{dt} = 100t^2 \qquad \frac{dP}{dt} = 200P \qquad \frac{dP}{dt} = 100P^2$ 

$$\frac{dP}{dt} = 200$$

$$\frac{dP}{dt} = 200t$$

$$\frac{dP}{dt} = 100t$$

$$\frac{dP}{dt} = 200F$$

$$\frac{dP}{dt} = 100P^2$$

4.4 Determine  $\frac{dz}{dt}$  if you know that  $z = xy^2$ , z = 3,  $y = \frac{1}{2}$ ,  $\frac{dx}{dt} = -2$ , and  $\frac{dy}{dt} = 5$ .

- 4.5 Free Response Question (FRQ) Practice in a bit!!
- 4.6 Given g(x) is a differentiable function about which little else is known other that g(-3) = 2 and g'(-3) = 7. Use the tangent line of g(x) at x = -3 to approximate g(-2.9).
- $\lim_{x \to 5} \frac{x^4 625}{x^2 25}$ 4.7