



When Substitution does NOT work.

$$\textcircled{7} \quad \lim_{x \rightarrow 6} \frac{x^2 + 36}{x - 6}$$

(If we substitute 6 in for x we get zero in denominator)

Factor

$$\lim_{x \rightarrow 6} \frac{(x-6)(x+6)}{x-6}$$

Now Substitute

$$\lim_{x \rightarrow 6} x+6 = 6+6 = \boxed{12}$$

$$(11) \lim_{x \rightarrow 0} \frac{\sqrt{x+25} - 5}{x}$$

mult by conjugate

$$\lim_{x \rightarrow 0} \frac{(\sqrt{x+25} - 5)(\sqrt{x+25} + 5)}{x}$$

only mult the conjugate $\lim_{x \rightarrow 0} \frac{x+25 - 25}{x(\sqrt{x+25} + 5)} = \lim_{x \rightarrow 0} \frac{x}{x(\sqrt{x+25} + 5)}$

$$\lim_{x \rightarrow 0} \frac{1}{\sqrt{x+25} + 5} = \frac{1}{25+5} = \boxed{\frac{1}{10}}$$

$$(15) \lim_{x \rightarrow 0} \frac{\frac{1}{x+1} - 1}{x}$$

get rid of $(x+1)$ in denominator by mult every term by $(x+1)$
(Like mult by common denom.)

$$\lim_{x \rightarrow 0} \left(\frac{\frac{1}{x+1} - 1}{x} \right) x+1$$

$$\lim_{x \rightarrow 0} \frac{1 - (x+1)}{x(x+1)}$$

$$\lim_{x \rightarrow 0} \frac{1-x-1}{x(x+1)} = \lim_{x \rightarrow 0} \frac{-x}{x(x+1)} = \lim_{x \rightarrow 0} \frac{-1}{x+1} = \frac{-1}{0+1}$$

$\boxed{-1}$